

Theory of magnetic field-stabilized compact skyrmions in thin film ferromagnets

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Compact magnetic skyrmions are potential bit-encoding states for spintronic memory and logic applications that have been the subject of a rapidly growing number of studies in recent years. Nevertheless, despite numerous attempts, a satisfactory theoretical description of these objects is still lacking today due to the highly non-trivial character of the magnetostatic interaction that plays a major role in determining the nature of magnetization patterns in ferromagnetic materials. The orthodox theory of skyrmions in ultrathin ferromagnetic layers with interfacial DMI relies on a model that accounts for the dipolar interaction through an effective anisotropy term, neglecting long-range effects. At the same time, in single ferromagnetic layers with interfacial DMI, large chiral skyrmions, also called skyrmionic bubbles have been observed, suggesting a non-trivial interplay between DMI and long-range dipolar effects [1]. We will present our work where we used rigorous mathematical analysis to develop a skyrmion theory that takes into account the full dipolar energy in the thin film regime and provides analytical formulas for compact skyrmion radius, rotation angle and energy [2]. Our theory reveals the existence of a new regime at low DMI where skyrmions are stabilized by a combination of non-local dipolar interaction and a magnetic field applied parallel to their core. This prediction is confirmed by our numerical simulations [3]. Finally, we will discuss the theory of skyrmion lifetime in a continuum field theory where we interpret skyrmion collapse events as capture by an absorber at microscale. This yields to an explicit Arrhenius collapse rate for skyrmions with both the barrier height and the prefactor as functions of all the material parameters [4]. Our work provides a guide in material system design in view of optimizing the skyrmion lifetime for applications.

References

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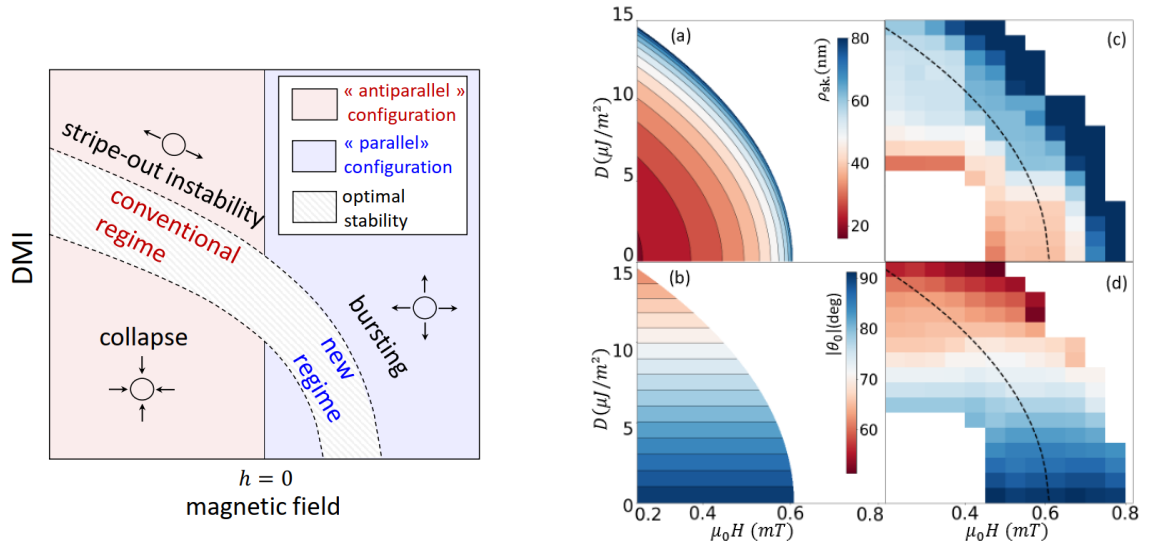


Figure 1: Left side: Schematic representation of the skyrmion phase diagram as a function of DMI and applied magnetic field where positive field is applied in the direction along with the magnetization in the skyrmion core (parallel configuration). We represent 3 types of skyrmion instabilities, stripe out, collapse and bursting as well as the optimal skyrmion stability zone. The new regime of field stabilized skyrmions is indicated. Right side: Analytical predictions of the skyrmion characteristics in the low DMI regime for $d = 5$ nm, $A = 20$ pJ/m, $M_s = 10^5$ A/m, and $K_u = 6346$ J/m³ corresponding to $Q = 1.01$: (a) Skyrmion radius r_{sky} and (b) skyrmion rotation angle. (c) skyrmion radius and (d) skyrmion rotation angle from MuMax3 simulations on a 2048×2048 nm² square box with mesh size $2 \times 2 \times 5$ nm. The dashed line is the line of zero bursting barrier.